

Interactions of traveling spots in a reaction-diffusion system

Kota Ikeda

Graduate School of Advanced Mathematical Sciences, Meiji University, Japan,

ikeda@isc.meiji.ac.jp

Reaction-diffusion systems can generate traveling spot solutions with a constant velocity. In the previous work [1], the interaction of spots is classified, and the explicit forms to describe the dynamics are obtained rigorously. Actually, some of traveling spot solutions exhibit spatiotemporal collective motions under the bifurcation structure with Jordan block type degeneracy. In this talk, we are concerned with the dynamics of spots near the bifurcation point. Using center manifold theory, we will reduce a reaction-diffusion system to an ordinary differential equation that describes positions and velocities of spots.

We also apply our result to the following system which is derived by modifying a model in [2];

$$(P) \quad \begin{cases} x_i'' = \gamma \left(\frac{1}{1 + au(x_i + r, t)} - \frac{1}{1 + au(x_i - r, t)} \right) - \mu x_i, & t > 0, \\ \frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} - ku + \sum_{i=1}^n F(x, x_i, r), & 0 < x < L, t > 0. \end{cases}$$

This model represents the self-sustaining motion of camphor disks in an annular water channel, where $x_i = x_i(t)$ and $u = u(x, t)$ denote the position of the i th camphor disks ($i = 1, \dots, n$) and the surface concentration of the camphor layer under periodic boundary conditions, respectively. The constants γ, a, μ, k are positive, and the function $F(x, x_0, r)$ is defined by

$$F(x, x_0, r) = \begin{cases} 1, & -r < x - x_0 < 0, \\ \rho, & 0 < x - x_0 < r, \\ 0, & |x - x_0| > r \end{cases}$$

for a positive constant $0 < \rho < 1$. We will characterize several types of solutions in a reduced system through bifurcation theory.

This is a joint work with Shin-Ichiro Ei (Kyushu University), Akiyasu Tomoeda (Meiji University, Science and Technology Agency CREST), and Masaharu Nagayama (Hokkaido University, Science and Technology Agency CREST).

References

- [1] *S.-I. Ei, M. Mimura, M. Nagayama*: Pulse-pulse interaction in reaction-diffusion systems. *Physica D* *165* (2002), 176–198.
- [2] *M. Nagayama, S. Nakata, Y. Doi, Y. Hayashima*: A theoretical and experimental study on the unidirectional motion of a camphor disk. *Physica D* *194* (2004), 151–165.